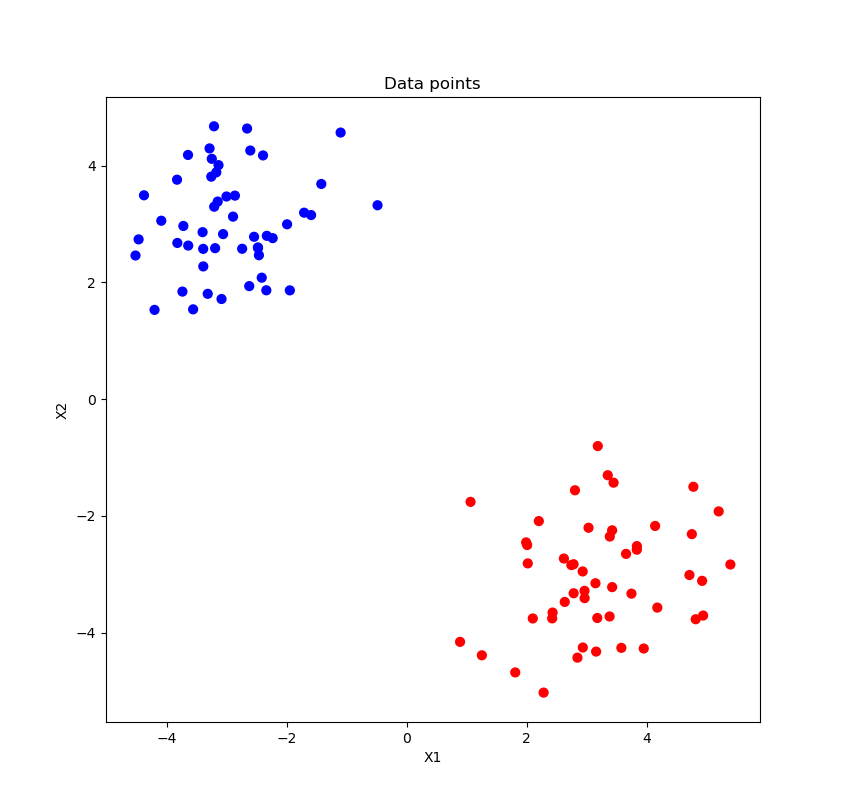
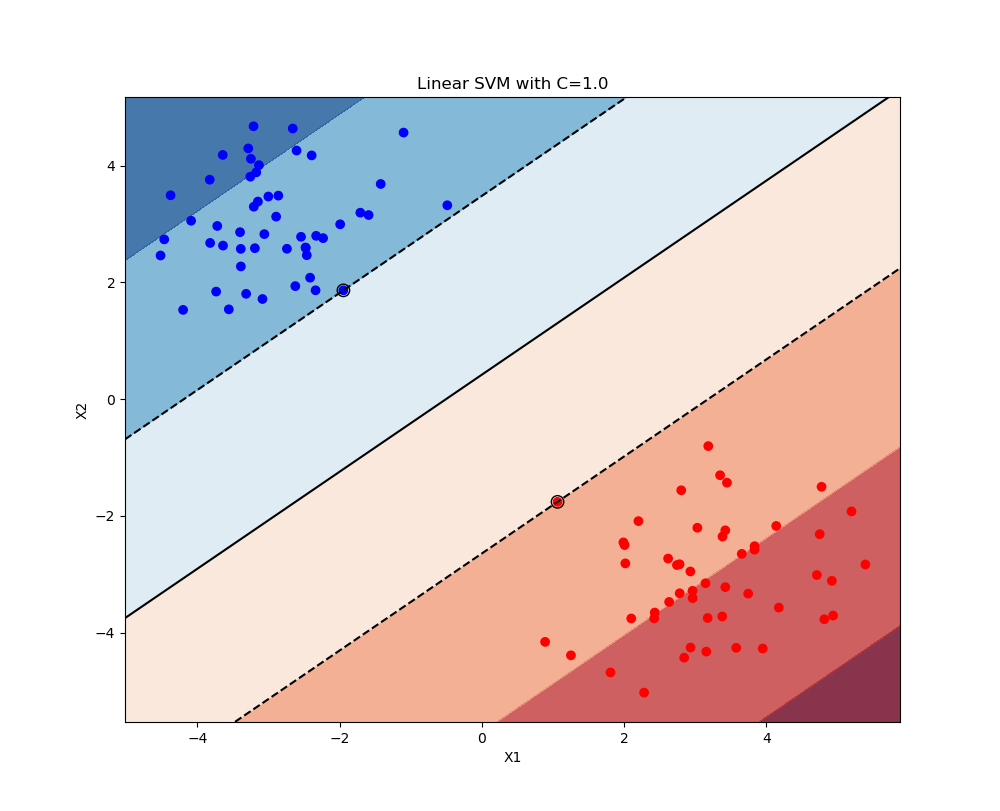
# Linear SVM

Here below the graph representing the dataset used for this section where different colors correspond to different labels.



## Ex\_1\_a

Here below the graph showing the result of the SVM trained with a linear kernel and the provided dataset.



## 1.2 Ex\_1\_b

The point added in this section is the blue point that is very far away from the others at the cords (4, 0) (label 1 so blue). As we can see this point is part of the blue group and not the red one it seems closer to. As we can see this point, being counted in the "blue dataset", leads to a modification of the decision boundary since it seems clear looking at the graph in section 1.1 that with the previous decision boundary would instead fall within the red group of points.

## 

## 1.3 Ex\_1\_c

As we can see in the graphs below, a high value of C contributes to a higher accuracy in the choice of decision boundary. In the chart resulting from C = 106 we can see that all points are on the right side of the decision boundary and there is no point between the margin (dashed line) and the boundary decision so we can consider all the points as support vector.

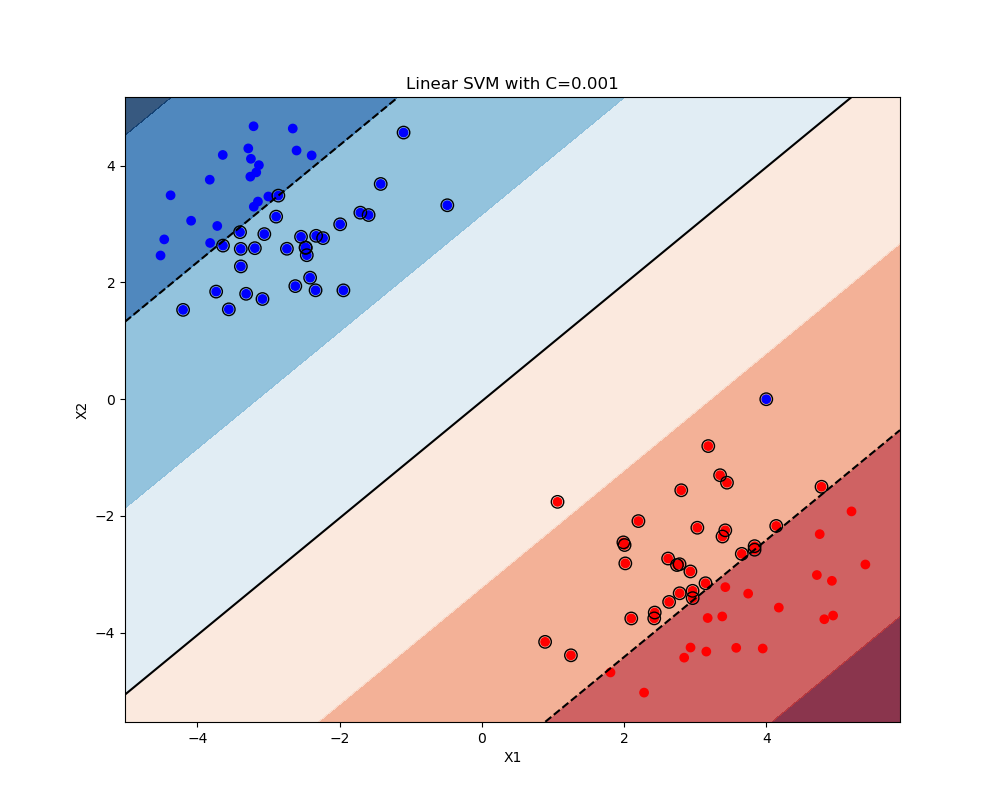
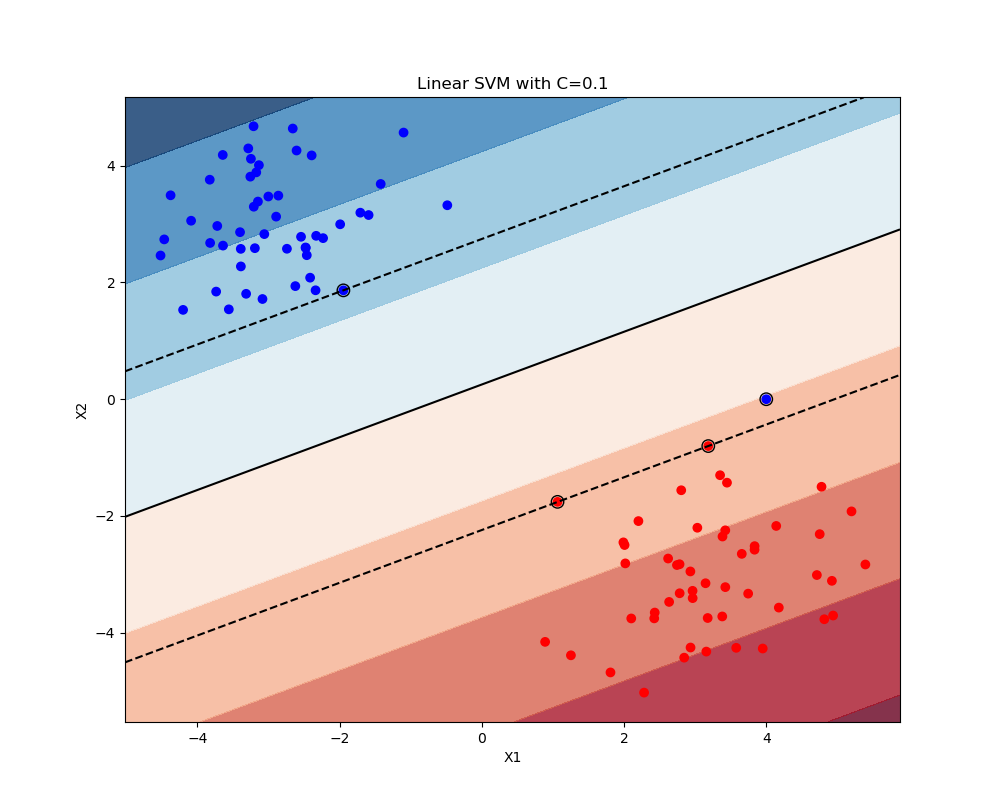
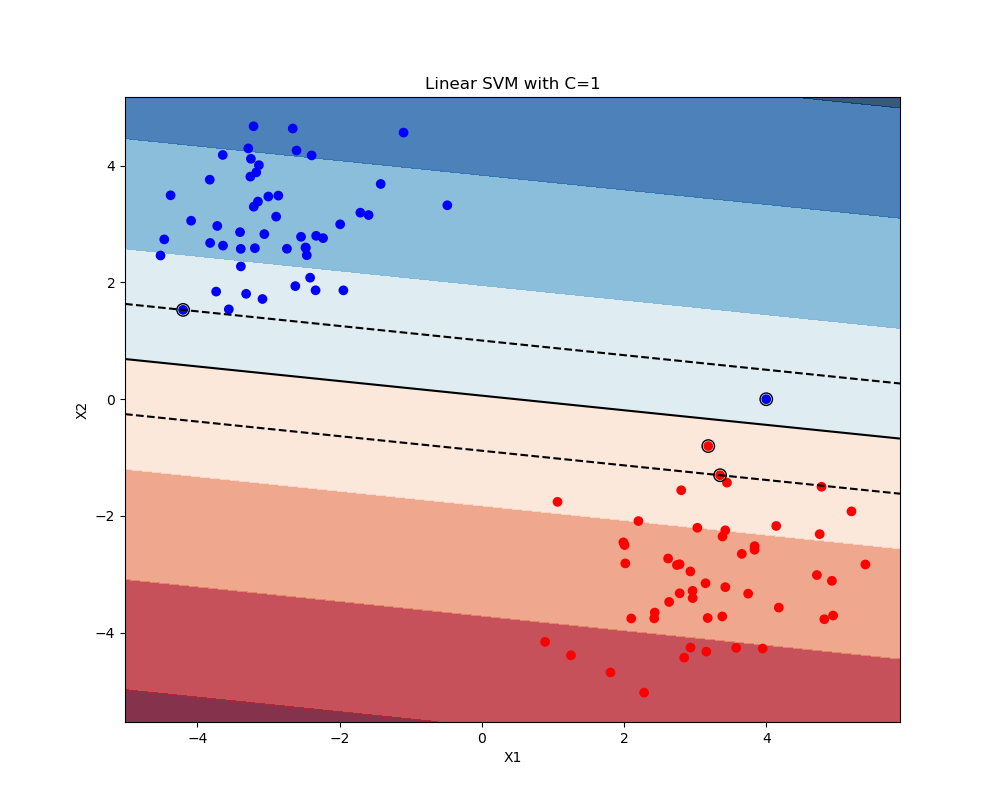
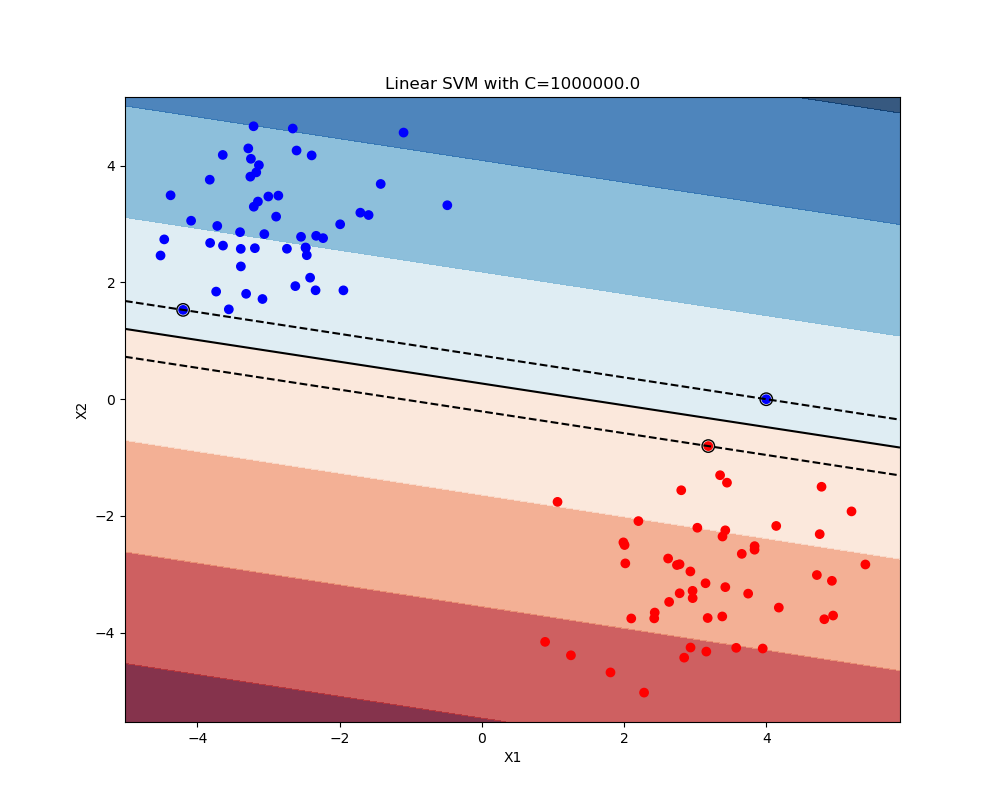
The second graph is the same graph of section 1.2 and present no points on the wrong side of the decision boundary but 2 points (one red and one blue) on the maximum-margin hyperplane (the two parallel hyperplanes that separate the two classes of data).

The third graph where C = 0.1 has instead a blue point (the added one) on the wrong side of the boundary (the red one).

Also the last graph has the added point on the red side of the boundary and presents a lot of points of both sides that are on the maximum-margin hyperplane.

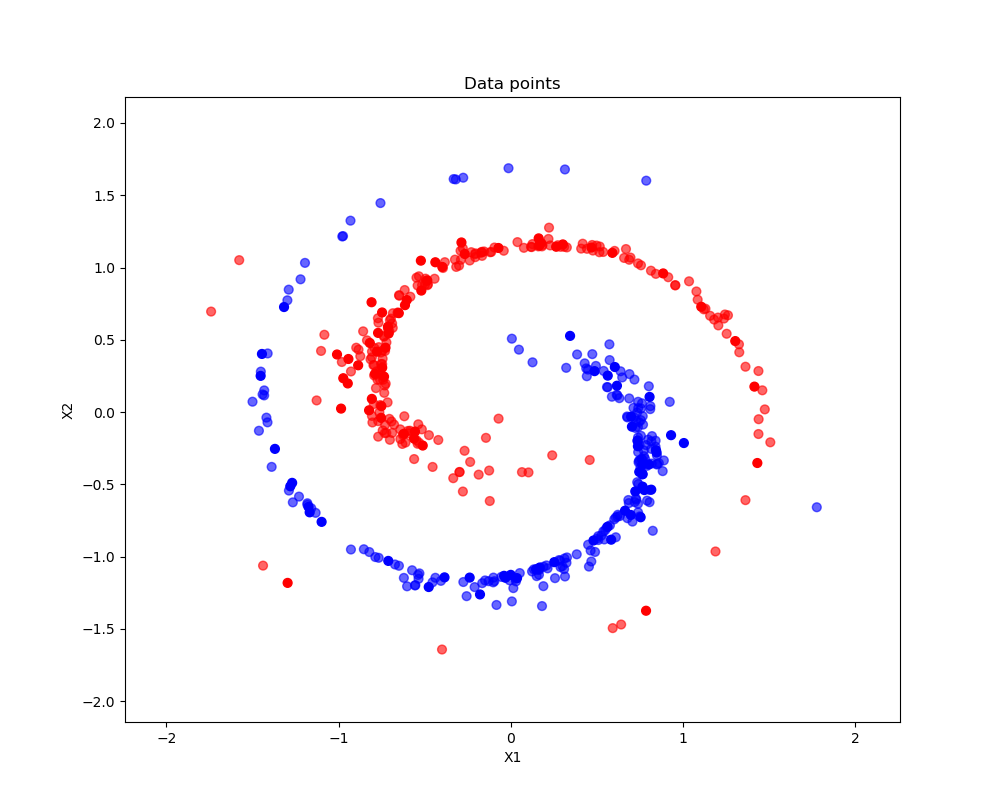
Interesting is to see that for C > 1 and C < 1 the slope of the boundary changed direction.

In this case we have seen that with a high value of C all the points result in support vector while with a too low value many points end up inside the maximum-margin hyperplane.

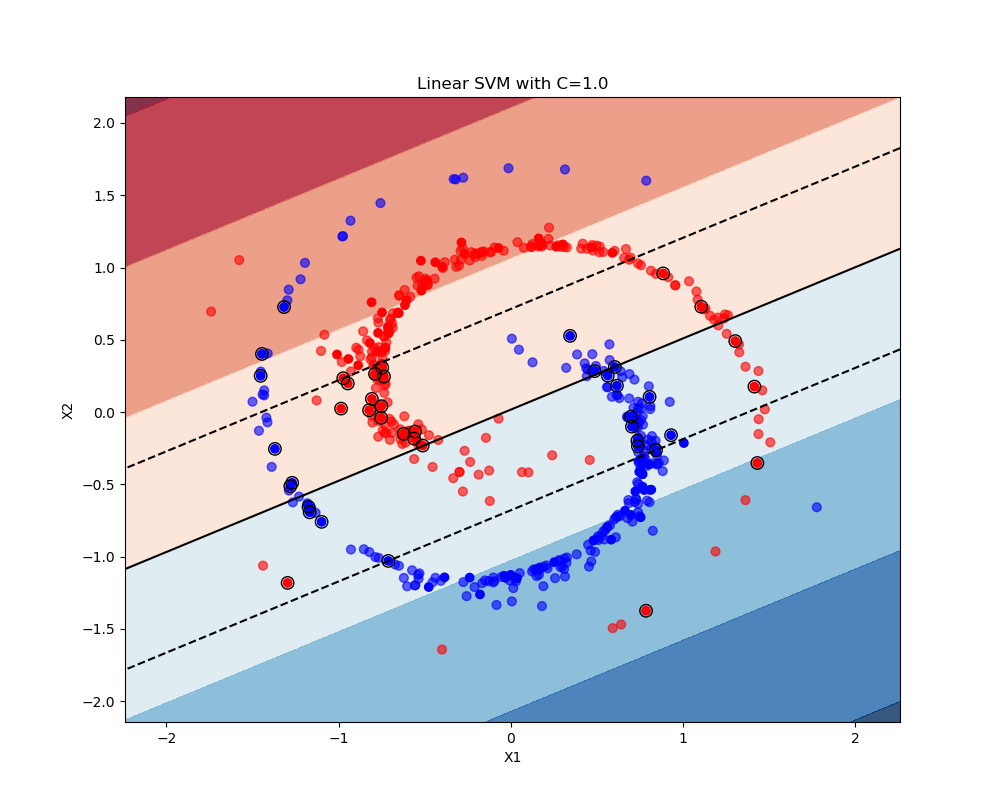


# Nonlinear (kernel) SVM

Here below the graph representing the dataset used for this section.

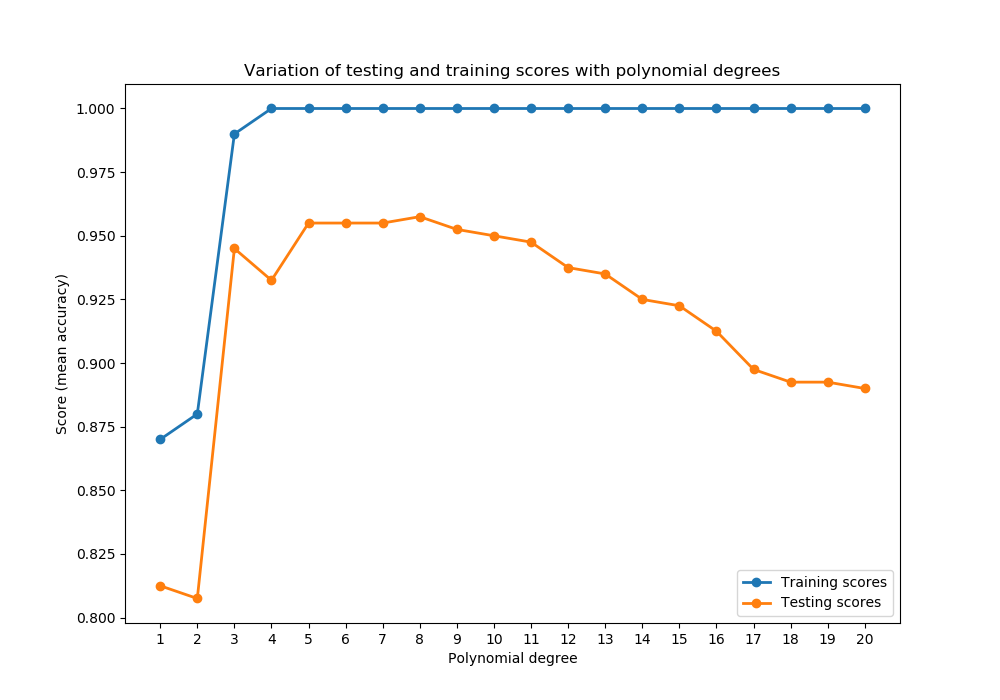


## Ex\_2\_a – Linear kernel

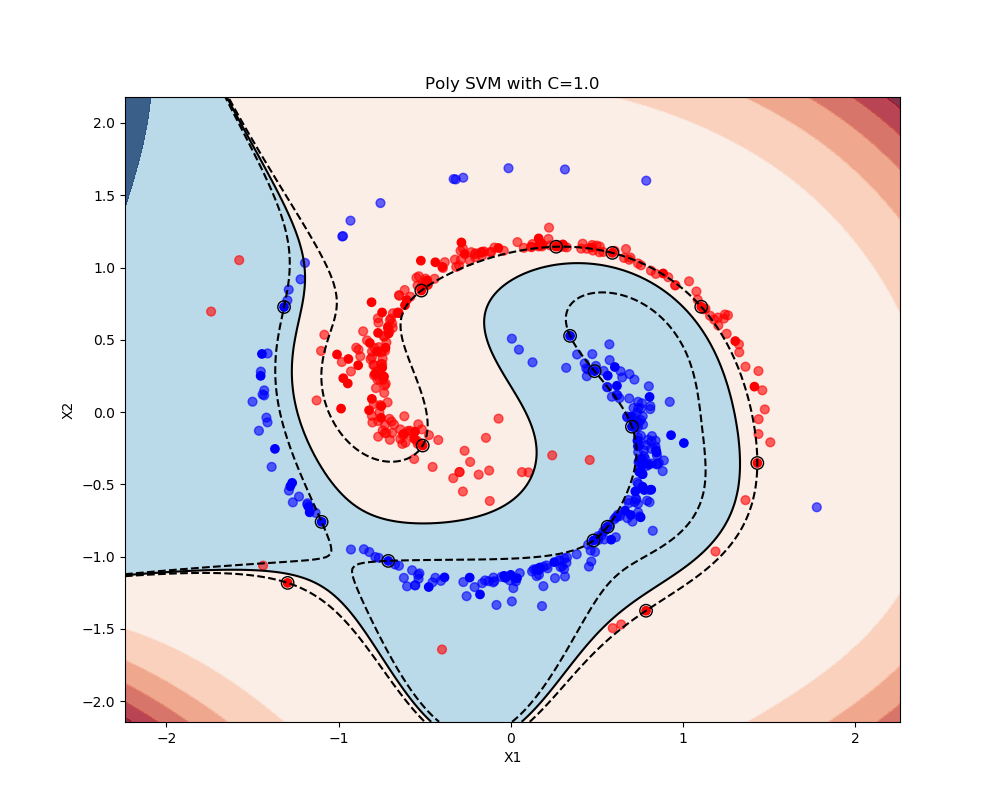


As we can see from the graph above the linear kernel is probably not the optimal kernel for this type of dataset which is very difficult to split into two sections with a linear boundary. The mean accuracy of classiﬁcation (obtained with the method score) for the testing set is 0.815 which is high but for sure not optimal.

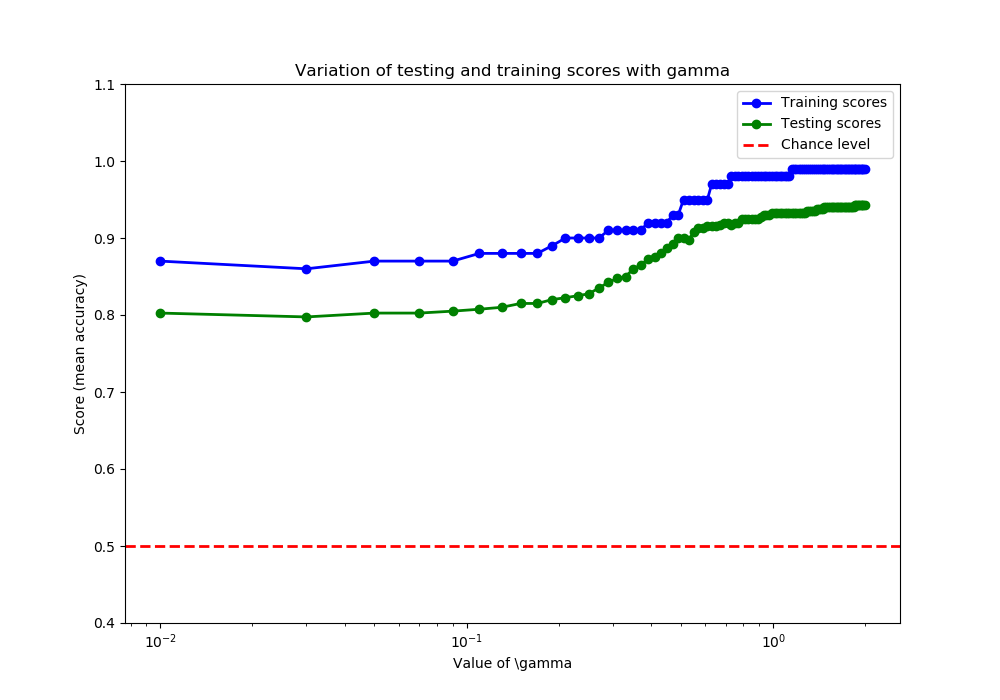
## Ex\_2\_b - Polynomial kernel

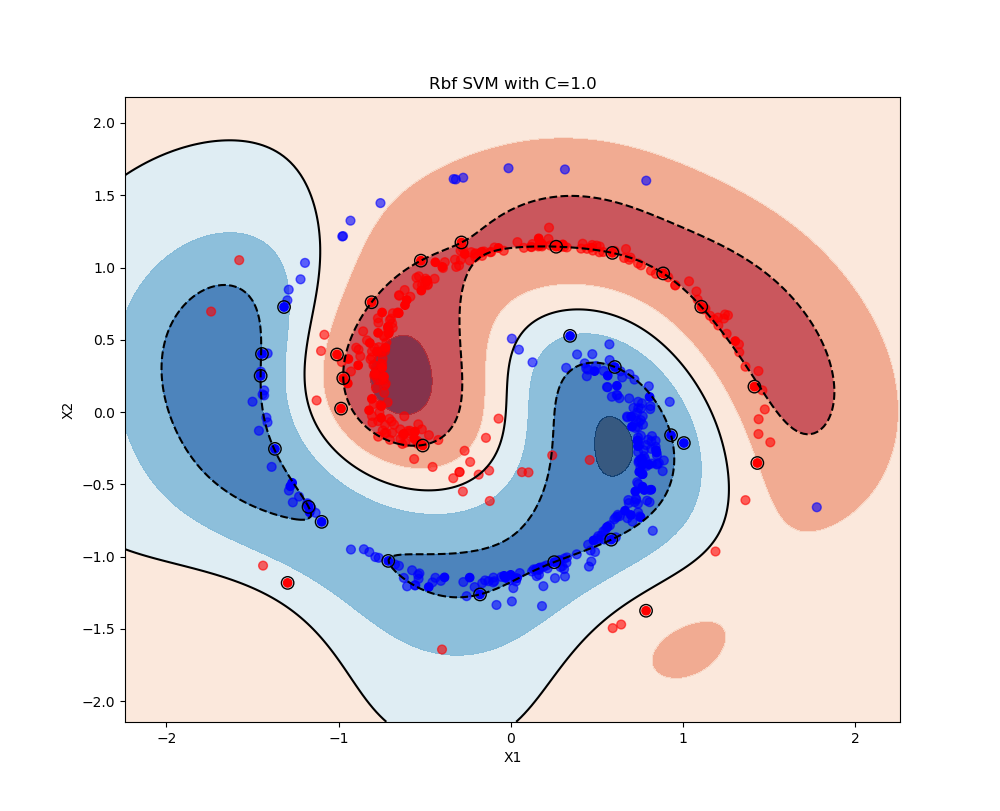


The graph above shows the mean accuracy of classification for each degree for both training and testing set. The optimal polynomial to describe this data set is the grade 8 polynomial shown below that presents an accuracy of 0.955 that is a lot better than the one obtained with the linear kernel. Interesting to see is also that the training set reach an accuracy of 100% already with a polynomial of grade 4 and then it stays costant.



## Ex\_2\_c – RBF kernel



The graph above shows the mean accuracy of classification for each value of gamma for both training and testing set. The optimal result is obtained with a gamma value of 1.8499e and has an accuracy of 0.9425. The graph for the optimal gamma is shown below. 

## Observations

* The polynomial kernel is performing the best as it has the best optimal score.
* As we can see from the graphs the more the decision boundary is complex more are the founded support vectors
* The RBF kernel is generalizing better than the others kernel as the behavior of the boundary seems more similar to the behavior of the points than the one of the other kernels